

# Towards a better understanding of Burrows's Delta for literary authorship attribution

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## Notation

- Text documents  $D$  in a collection  $\mathcal{D}$  of size  $n_{\mathcal{D}}$
- Each text  $D$  is represented by a profile of relative frequencies  $f_i(D)$  of the  $n_w$  most frequent words  $w_1, w_2, \dots, w_{n_w}$
- The complete profile of  $D$  is given by the feature vector  $\mathbf{f}(D) = (f_1(D), \dots, f_{n_w}(D))$
- Features are standardized using a z-transformation  $z_i(D) = \frac{f_i(D) - \mu_i}{\sigma_i}$
- Dissimilarities between the scaled feature vectors are computed according to a distance metric

## Delta Measures

- Burrows's Delta [1]: Manhattan Distance

$$\Delta_B(D, D') = \|\mathbf{z}(D) - \mathbf{z}(D')\|_1 = \sum_{i=1}^{n_w} |z_i(D) - z_i(D')|$$

- Quadratic Delta [2]: squared Euclidean Distance

$$\Delta_Q(D, D') = \|\mathbf{z}(D) - \mathbf{z}(D')\|_2^2 = \sum_{i=1}^{n_w} (z_i(D) - z_i(D'))^2$$

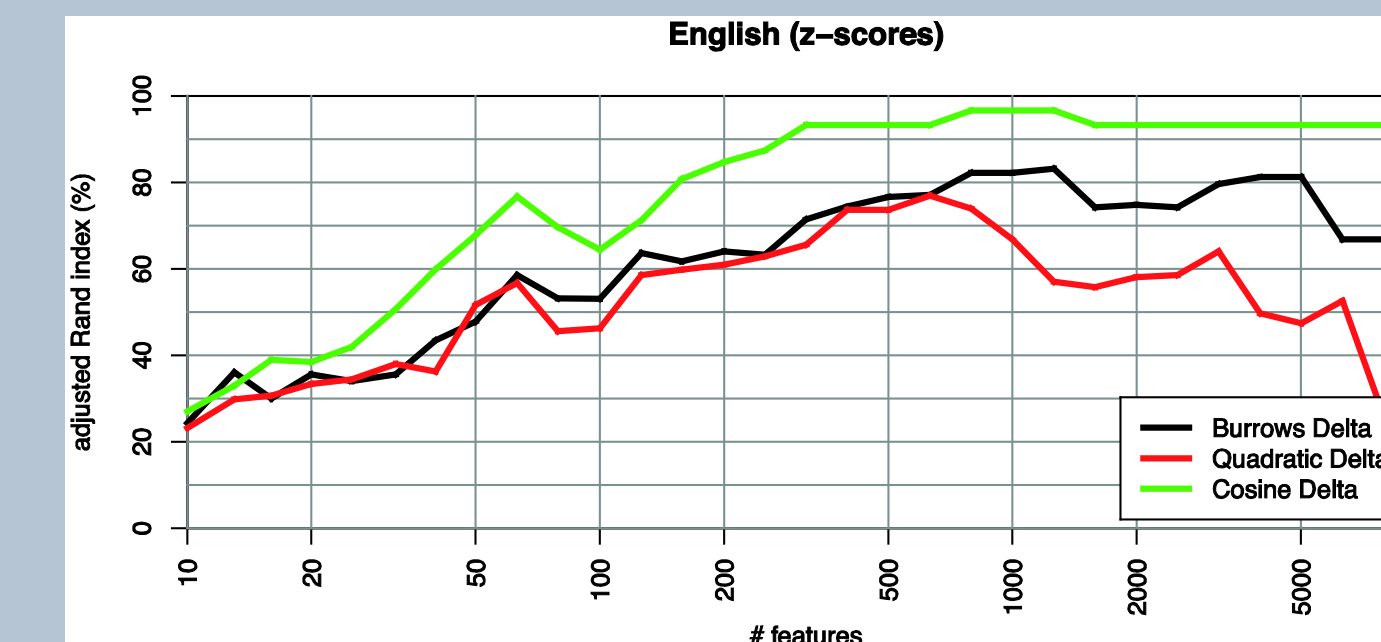
- Cosine Delta [3]: angle  $\alpha$  between two feature vectors, computed from cosine similarity of  $\mathbf{x} = \mathbf{z}(D)$  and  $\mathbf{y} = \mathbf{z}(D')$

$$\Delta_{\angle}(D, D') = \alpha, \text{ with } \cos \alpha = \frac{\mathbf{x}^T \mathbf{y}}{\|\mathbf{x}\|_2 \cdot \|\mathbf{y}\|_2}$$

## Understanding the parameters of Delta

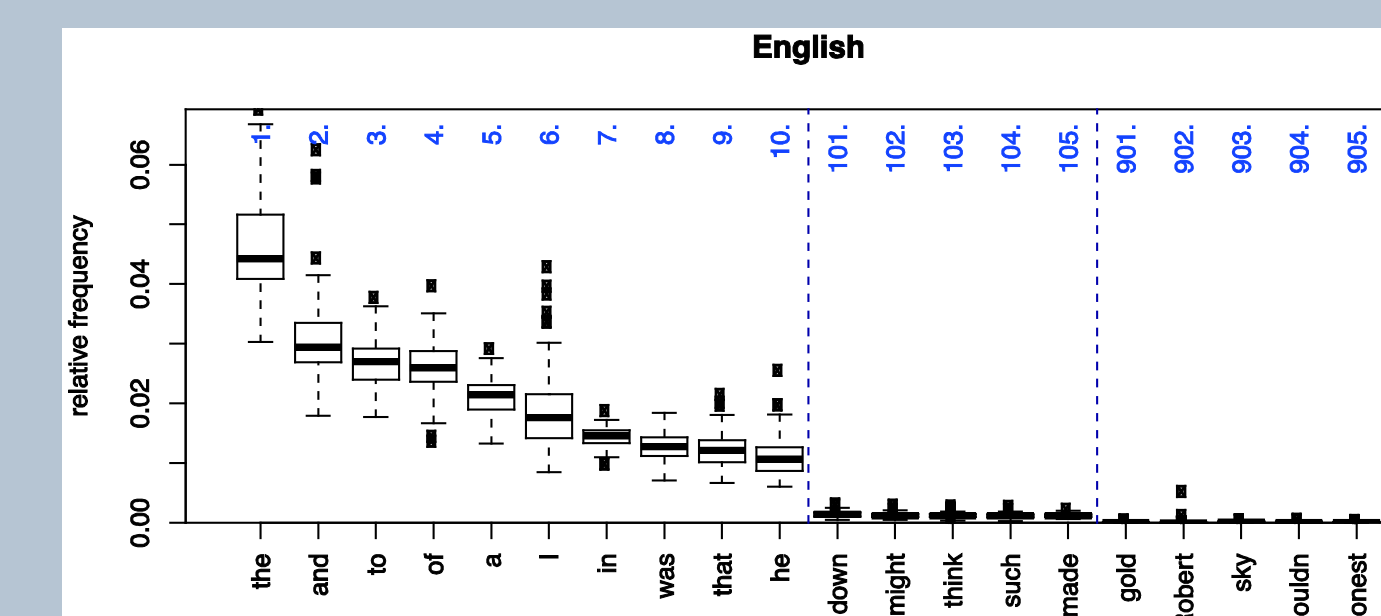
### MFW

- Same clustering quality for  $\Delta_B$  and  $\Delta_Q$  for  $n_w \leq 500$ , but  $\Delta_B$  proves to be more robust if  $n_w$  is increased, cf. [4]
- $\Delta_{\angle}$  outperforms the other variants, is robust, degrades more slowly and achieves impressive clustering quality
- Optimal  $n_w$  depends on many factors (language, text type, text length,...) and cannot be known a priori



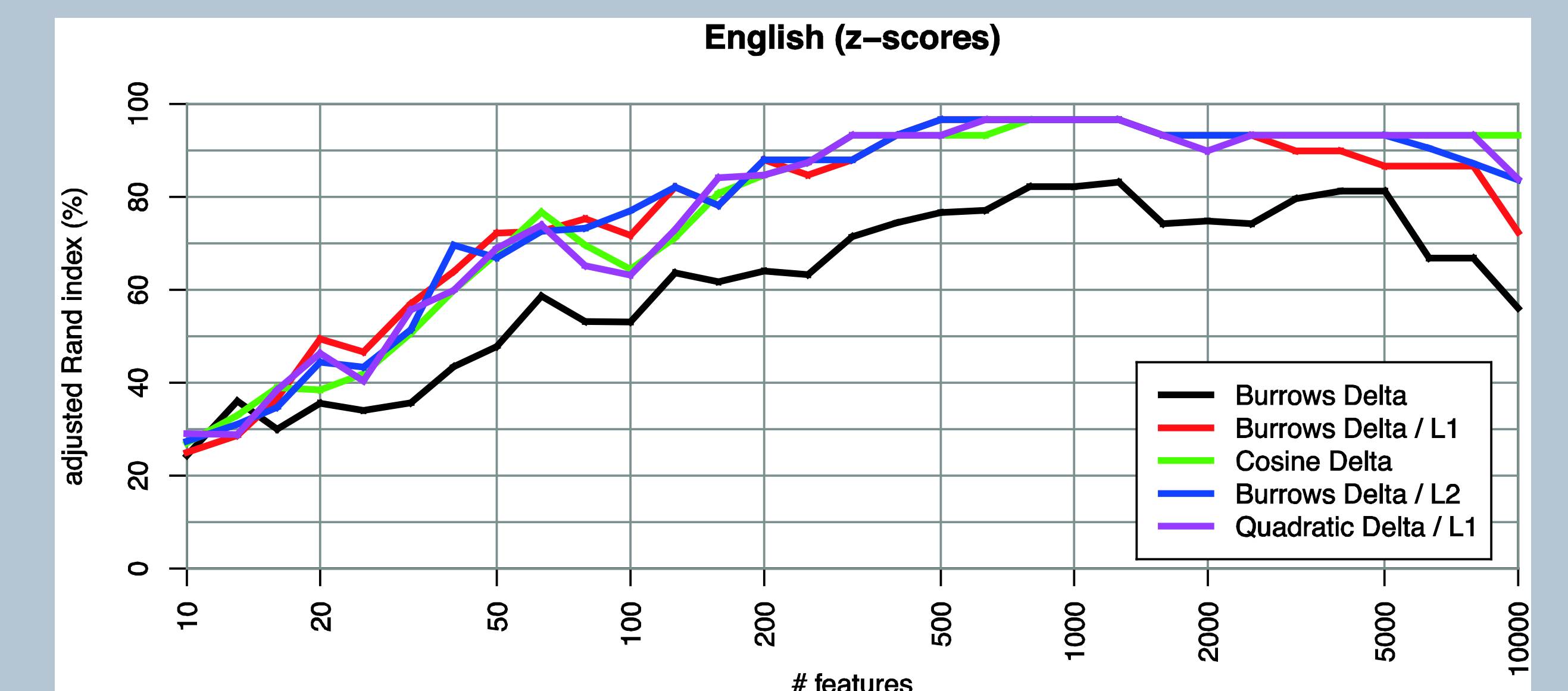
### Feature scaling

- Without standardization, words with mfw ranks above 100 hardly make any contribution to the frequency profiles and hardly affect the delta scores
- Standardization gives all features equal weight in  $\Delta_Q$  and  $\Delta_{\angle}$
- In  $\Delta_B$ , standardization gives less frequent words a moderately smaller weight; it also reduces the weight of words concentrated in a small number of texts. Experiments show that this results in better clustering quality than a scaling that gives equal weight to all features.



### Vector normalization

- Normalization is the main difference between  $\Delta_Q$  and  $\Delta_{\angle}$ , might also improve other measures
- $\Delta_Q$  and  $\Delta_B$  are substantially improved by vector normalization, regardless of the type of normalization ( $L_1$  vs.  $L_2$ )
- Authorial style reflected by positive and negative deviations of word frequencies from the average frequency across the collection
- Not to the same degree in all texts of one author, therefore differences in length (i.e. norm) of feature vectors
- Normalization makes the author's stylistic pattern stand out more clearly



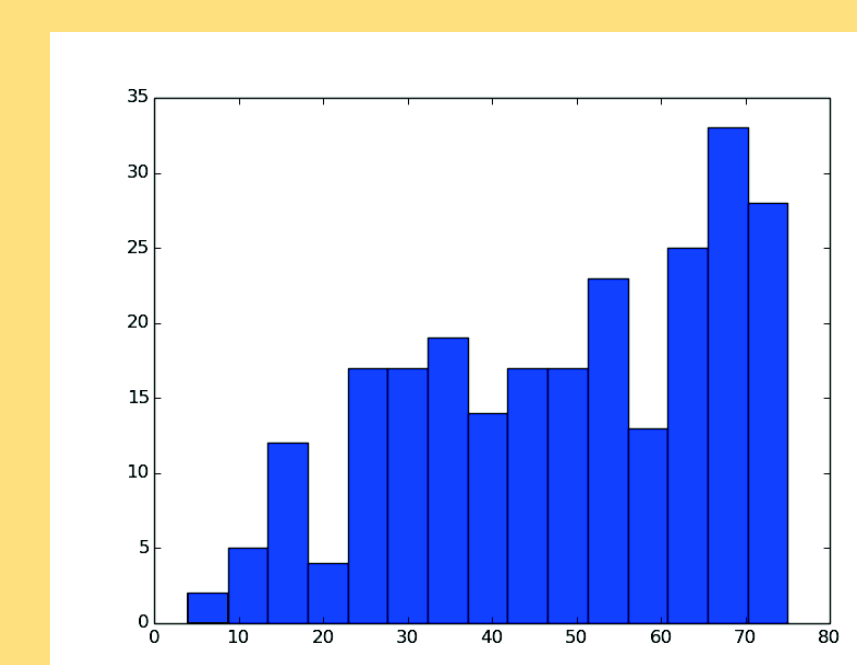
## Recursive feature elimination

- Greedy algorithm which relies on a ranking of features and on each step selects only the top features, removing the remaining ones
- Reduction to 50000 features in steps of 10000, to 5000 in steps of 1000 and finally to 500 in steps of 100 features
- Find the optimal number of features by pruning one feature at a time with stratified threefold cross-validation after each step
- Both classification and clustering with  $\Delta_{\angle}$  with optimal feature subset yield perfect results

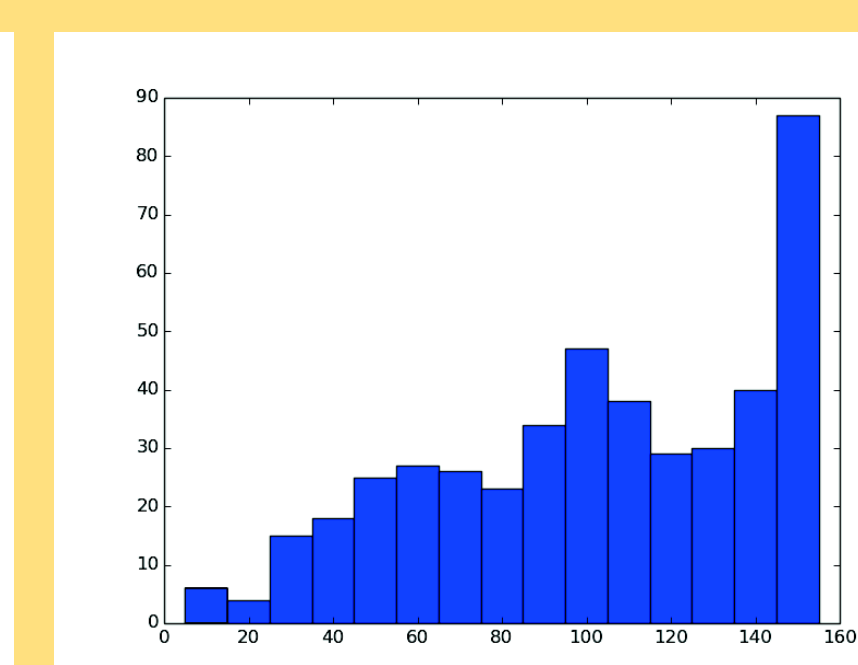
	English	French	German
nr. of features	246	381	234
SVC accuracy	0.99 ( $\pm 0.04$ )	1.00 ( $\pm 0.00$ )	1.00 ( $\pm 0.00$ )
MaxEnt accuracy	1.00 ( $\pm 0.00$ )	1.00 ( $\pm 0.00$ )	1.00 ( $\pm 0.00$ )
Cosine Delta ARI	0.966	1.000	1.000

## The selected feature subset

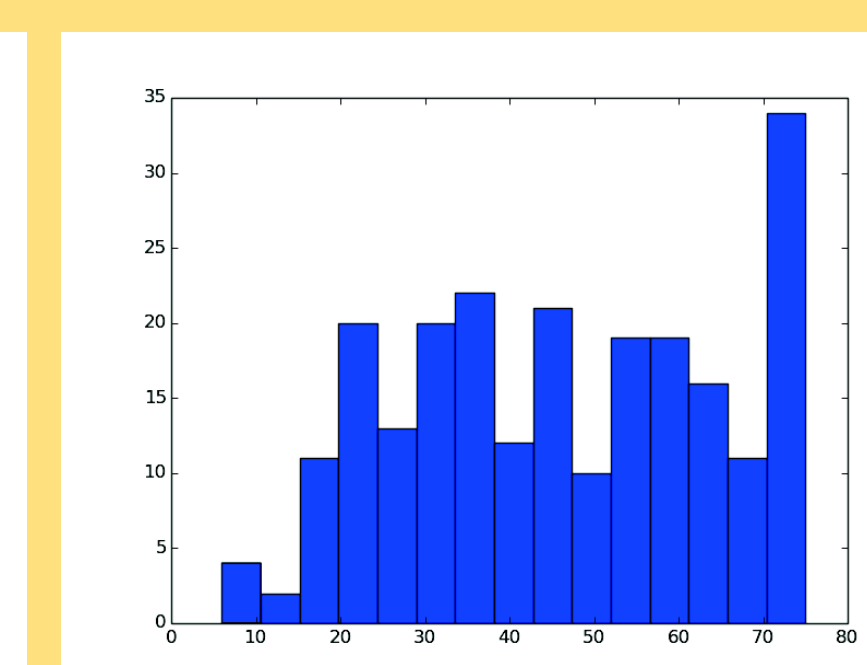
- Some features highly specific, occurring only in a fraction of texts, but most selected features have a rather high document frequency
- Not limited to function words
- Roman numerals in French and English collection characteristic of novels with unusually many chapters
- Artifacts in German collection due to historic orthographic variants



(a) English



(b) French



(c) German

## Possible overfitting?

- Two additional unseen evaluation data sets, the second mainly consisting of additional authors
- Classification accuracy of 0.97 on first test set indicates good generalization to unseen works from the same authors
- Classification and clustering with  $\Delta_{\angle}$  on the set with new authors and no singletons also yield good results
- Higher ARI for selected features than for 2000 mfw indicates that features are not overfitted and generalize well to unknown authors
- Difference in accuracy between the first and second test set indicates that features are somewhat author-dependent

	unscaled full fs	rescaled full fs	selected fs
SVC accuracy	0.91 ( $\pm 0.03$ )	0.57 ( $\pm 0.13$ )	0.84 ( $\pm 0.14$ )
MaxEnt accuracy	0.95 ( $\pm 0.03$ )	0.95 ( $\pm 0.03$ )	0.90 ( $\pm 0.08$ )
Cosine Delta ARI	0.835	0.835	0.871

## References

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- Fotis Jannidis, Steffen Pielström, Christof Schöch and Thorsten Vitt. 2015. Improving Burrows's Delta – An empirical evaluation of text distance measures. In *Digital Humanities Conference 2015*, Sydney.

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